

Time : Three Hours] [Maximum Marks : 75

Note: Attempt Five questions in all, selecting at least one question from each Unit. All questionscarry equal marks.

Unit I

- (a) In a survey of 60 people, it was found that : 25 read Newsweek magazine, 26 read Time, 26 read Fortune, 9 read both Newsweek and Fortune, 11 read both Newsweek and Time, 8 read both Time and Fortune, 3 read all three magazines. 10 (i) Find the number of people who read at least one of the three magazines.
 - (ii) Find the number of people who read exactly one magazine.
 - (iii) Find the number of people who read Newsweek and Time but not all three magazines.

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- (iv) Find the number of people who read Newsweek and Fortune but not all three magazines.
- (v) Find the number of people who read Fortune and Time but not all three magazines.
- (vi) Find the number of people who read only Newsweek.
- (vii) Find the number of people who read only Time.
- (viii) Find the number of people who read only Fortune.
- (ix) Find the number of people who read no magazine at all.
- Also draw a Venn diagram of the above problem.) Determine whether or not $-p \odot (pv \sim p)$ is a tautology or contradiction.
- 2. (a) Prove that (ah)'' = a''b'' is true for every natural number n. 7
 - (b) What are normal forms ? Discuss its various types using suitable examples. 8

Unit II

 (a) Prove that (D30) is a lattice. Also draw a hasse diagram of D30, 7
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- (b) Let y = {a, 6}. Define a relation R on £⁺ as xRy if x is a prefix of y. Is R a partial order ? 8
- (a) Write down the Warshall's algorithm for finding the shortest path. Explain the algorithm using suitable examples. 10
 - (b) Let $A = \{0, 1, 2, 3\}$ and let $r = \{(0, 0), (1, 1), (2, 2), (3, 3), (1, 2), (2, 1), (3, 2), (2, 3), (3, 1), (3, 2), (2, 3), (3,$
 - (I, 3)).
 (I) Show that r is an equivalence relation on A.
 (II) Let a belongs to A and define c(a) = 16 belongs to A | a r b], c (a) is called the equivalence class of the elements a under r.
 - Find c(a) for each element a belonging to A.

Unit III

- (a) Using generating functions, solve the recurrence relation a_n =ba_n_\-9an_2, where a0 = 2 and a_n = 3.
 - (b) Prove that 'A function /: A → B is invertible if and only if both one-to-one and onto'. 8

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 (a) Each user on a computer system has a password, which is six to eight characters long, where each character is an uppercase letter or a digit. Each password must contain at least one digit. How many possible passwords are there ? 10
 (b) State and prove Pigenohe principle. 5

Unit IV

- (a) Define a semigroup and a group and prove that a semi-group G is a group if and only if the equations ax = b and ya = b has solutions in G for arbitrary a, b e G
 - (b) Define homomorphism and its properties. Check whether 0 : <u>Z5</u> -> <u>Z2</u> is defined by <u>Q(n) = 0</u> if n is even and 0(h) = 1 if h is odd. 8
- (a) Consider the group G = [1, 2, 3, 4, 5, 6) under multiplication modulo 7.
 (i) Find the multiplication table of G
 (ii) Find inverse of 2, 3, 6.
 (iii) Find the orders and subgroups generated by 2 and 3.
 (iv) Is G cyclic ?
 (b) Prove that H, a subset of group [G; *] is a subgroup.
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